

A Classification Model for Imbalanced Medical Data based on PCA and Farther Distance based Synthetic Minority Oversampling Technique

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Abstract—Medical data are extensively used in the diagnosis of human health. So it has played a vital role for physicians as well as in medical engineering. Accordingly, many types of research are going on related to this to have a better prediction of the diseases or to improve the diagnosis quality. However, most of the researchers work on either dimensionality space or imbalanced data. Due to this, sometimes one may not have the accurate predictions or classifications of the malignant diseases as both the factors are equally important. So it still needs an improvement or more work required to address these biomedical challenges by combing both the factors. As such this paper proposes a new and efficient combined algorithm based on FD_SMOTE (Farther Distance Based on Synthetic Minority Oversampling Techniques) and Principle Component Analysis (PCA), which successfully reduces the high dimensionality and balances the minority class. Finally, the present algorithm has been investigated on biomedical data and it gives the desired results in terms of dimensionality and data balancing. Here, In this paper, the quality of dimensionality reduction and balanced data has been evaluated using assessment metrics like co-variance, Accuracy (ACC) and Area Under the Curve (AUC). It has been observed from the numerical results that the performance of the algorithm achieved the best accuracy with metrics of ACC and AUC.

Keywords—Principle Component Analysis; Information Gain; farther Distance based Synthetic Minority Oversampling; Correlation based Feature

I. INTRODUCTION

Classification is an important task of machine learning and data mining. Classification modeling is to learn a function from training data, which makes as few errors as possible when being applied to data previously unseen. A large number of classification algorithms have been developed and used with medical applications, due to its importance for physicians in the diagnosis. Many researchers have been done to discuss the great challenges of the medical data. Imbalance class is the

main challenge that influences to the classification of the medical data. In many cases, the nature of medical data follows the skewed distribution. Its instances in the majority and minority classes are not equality represented [1, 2]. Hence, the medical data becomes imbalanced when its majority class has a larger number of instances. With the traditional classification algorithms obtain a higher accuracy over majority while Versa with minority class. For this reason, new techniques and methods for dealing with class imbalance have been proposed [9]. These techniques can be classified into three methods: those that amend the data distribution by resampling techniques (data level methods) [11], and those at the level of the learning algorithm which adapt a base classifier to deal with class imbalance (algorithm level methods), and those at the features selection level which find an optimal features among the whole the features. In this paper, we proposed a combined solution to classify imbalanced data, which successfully reduces dimensionality, and balances the minority class using a combination of Principle Component Analysis (PCA) and Synthetic Minority Oversampling Techniques. The innovation of this proposal is the joint utilization of both (PCA) and FD_SMOTE techniques, which achieved superior results in our experiment. In this paper, the quality of dimensionality reduction and balanced data has been evaluated using assessment metrics like Co-variance, Accuracy (ACC), and Area Under the Curve (AUC). It has been observed from the numerical results that the performance of the algorithm achieved the best accuracy with metrics (ACC) and (AUC). Finally, the FD_SMOTE technique has been investigated on biomedical data, and it realized the desired results in terms of dimensionality and data-balancing.

This paper is organized as follows. In Section 2 background of the present study with the literature review has been presented. After that in Section 3 existing approaches have been discussed. Next in Section 4, a new method has been proposed with experimental analysis. Lastly Section 5 includes the conclusion part.

II. BACKGROUNDS

Imbalanced data is the most important issue in all applications of the real world, and the classification accuracy based on minority class can get a higher priority than that majority class, so it is a significant work to enhance the classification precision of minority class. In this section, we will explain the basic concept of the problem and the associated solution.

A. Imbalanced Data Problem

Sun et. al stated that the most understandable problem in data set is the imbalance data distribution between classes [10]. Nevertheless, the earlier studies and research stated that the imbalanced data distribution is not only the main issue that reduces the performance of the existing classifiers in specifying rare samples. The other influential issue of the classifier performance is small samples size, separability and the existence of within-class.

B. Presented Approach of Imbalanced Data Problem

There are different approaches have been presented to tackle the imbalance class problem [7], [8,] [9], which can be categorized as a resampling approach, algorithms approach and features selection approach.

- The preprocessing approach is a combination of over-sampling technique and under-sampling technique. The Oversampling is a powerful method used to add new samples, while under-sampling is a process of removing existing samples. These techniques mostly fix the imbalance data by generating or updating some of the classifiers algorithms. The classification algorithm should include the cost sensitivity, recognition-based approaches, and kernel-based learning techniques, which perfectly provide an acceptable solution for the imbalanced data problem. The support vector machine SVM is one of the most popular algorithms that embed the previous techniques [9]. Due to a large amount of bio-medical data and class imbalance ratio, applying the algorithm alone is not a good idea. Hence new hybrid approaches are required as a combination of sampling techniques and algorithms [10].
- The algorithms approach is the most popular technique that has been used to fix the imbalanced data problem, which is the bias towards the majority class and ignoring the minority class. The correct classification of the minority class gives a better accuracy, while in many applications, misclassification of minority class results in serious problems [11]. The inaccurate classification of the benign disease leads to additional diagnosis, while the inaccurate classification of malignant disease puts the human life at serious risk. Therefore, most of the machine learning algorithms tries to enhance the inaccurate classification of the minority class.
- The feature selection approach has been presented as a good solution for bio-medical data with a large amount. The size of this data can be reduced to a lower

space dimension using linear transformation or non-linear transformation which is used based on its linearity nature. Imbalanced data on minority class and high dimensionality problem causes a misclassification. This misclassification of entities that have the same attribute value could disturb the diagnoses of diseases. For example, the boundaries between a malignant headache and a brain tumor could be vague under some circumstances, which is obviously catastrophic. Therefore, it is not easy for the medical doctors to examine the abnormalities in human in the misclassified data. The hybridized of reduction dimensionality and balance data technique is necessary in most bio-medical applications in order to enhance and recover misclassifications details that may be hidden in the data [3][4].

III. THE PROPOSED METHOD

The proposed method provides an accurate classification model by using a combination of the PCA and SMOTE technique. The PCA is used to reduce the high dimensionality of data by select an optimal feature from the original data set. The PCA generate a new dimension space of the data which implemented with the FD_SMOTE to balance the data of the minority class, while the imbalanced data split into train and test data, and then the balanced data applied to the different classifiers to achieve the better classification for the medical data.

A. Principle Component Analysis

In the proposed model the features selection is used as the key technique to find a subset of optimal features from the original data. The extracted features allow the classifier to achieve the best accuracy. Here, PCA to reduce the high dimensional point into lower dimensional point and then using filters to order the importance of the selected attributes based on a rule [5]. In this model, the dimensionality reduction has been implemented based some metrics such as mean, covariance, eignvalue and Eigenvectors to compute the principle component. Finally, the PCA provide a new transform of PCs which generated by using correlation matrix of the data to find the best PCs among all the features. These steps well explained in the algorithm 1.

$$C = \frac{1}{N} \sum_{j=1}^N \varphi_j \varphi_j^T = \rho \rho^T \quad (1)$$

$$\rho = \left(\varphi_1 \varphi_2 \dots \varphi_j \right) \quad (2)$$

$$\varphi = \nu_j - \mu \quad (3)$$

$$\mu = \frac{1}{M} \sum_{i=1}^M \nu_i \quad (4)$$

Where ν_i is a vectors from the original dataset X_i , and μ is mean of Jth vectors of the data, where φ is a variance of the vectors that subtracted from mean, and Then C is a covariance matrix which generated by multiplication of variance

with its variance transpose as $\varphi \times \varphi^T$. Finally, the eigenvalue λ and Eigenvectors ν can be easily substituted according to the co-variance matrix C to achieve new principle component.

B. Farther Distance based SMOTE

The SMOTE technique provides an optimal solution for imbalanced data distribution problem based on oversampling technique. The basic assumption of the SMOTE based on how to find the similarities of the feature among the minority class instance. The assumption is achieved by calculating the centroid [c] of the minority class sample and the distance [di] between all the minority sample and its centroid, then compute the average [avg] of distance matrix and the seed sample represented as a farther distance to the class center [c] and greater than the average distance [avg]. The new synthetic sample has been generated randomly by select one of the N-centriod, then multiply the difference between the seed sample and centriod with a random number σ between [0, 1] and then added to the original seed. Finally, the mathematical steps of the algorithm illustrated as follows:

$$c = \frac{1}{n} \sum_{i=1}^n y_i \tag{5}$$

$$d_i = (y_i - c) \tag{6}$$

$$avg = \frac{1}{n} \sum_{i=1}^n d_i \tag{7}$$

$$Ss = \{y_i | d_i > avg\} \tag{8}$$

$$nss = Ss_i + (Ss_i - c) \times \sigma \tag{9}$$

The FD_SMOTE work on creation of new examples instead of duplicating the minority class samples, as shown in Figure 1, the new “synthetic” examples are being created in the neighborhood of minority classes. Where the synthetic examples are generated operating in “feature space” rather than operating in “data space”. Along the line segment, each minority class has been taken and introducing synthetic examples to join all minority class nearest neighbors. The numbers of required synthetic example vary situation to situation so according to the requirement the numbers of k minority classes are chosen to generate the nearest neighbor synthetic example. Finally, the pseudo code the proposed method illustrated as in algorithm 2.

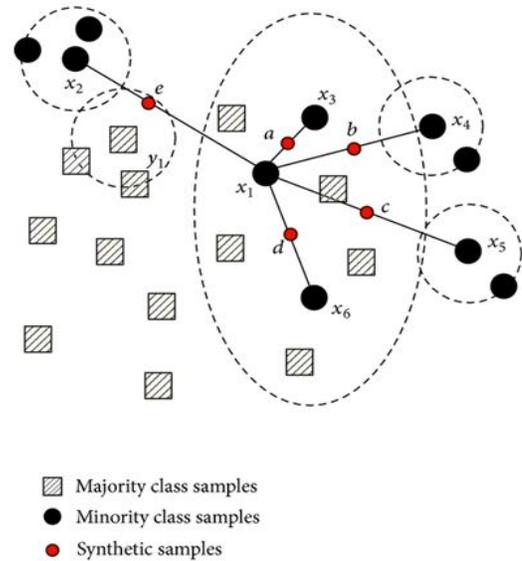


Fig. 1. FD_SMOTE Technique

Algorithm 1. Principle Component Analysis

- Input:** Original data set $\{X_i | i = 1, 2, \dots, m\}$, which each sample has m attributes without decision attribute.
Output: Principle Component $\{Y_i | i = 1, 2, \dots, n\}$,
 1: Victories the data into $V_i \dots \dots V_m$
 2: **for** $j \rightarrow n$ **do** jth is all vectors
 3: **for** $i \rightarrow m$ **do** ith instances of V_i
 4: Compute the mean according to Eq.(7)
 5: Subtract the instances according to Eq.(6)
 6: **end for**
 7: Multiply the variance according to Eq.(5)
 8: Compute the convince according to Eq.(4)
 9: **end for**
 10: Compute the eignvalue λ according to Eq.(4)
 11: Compute the eigenvectors ν according to Eq.(4)
 12: Output new Principle Component of features

Algorithm 2. FD_SMOTE resampling

- Input:** Origin set of minority, $D_{min} = \{Y_i | i = 1, 2, \dots, n\}$, the balance factor σ
Output: New et of minority, $D_{maj} = \{Z_i | i = 1, 2, \dots, m\}$
 1: Compute c , d_i and avg according to Eqs. (5), (6) and (7)
 2: Create seed sample according to Eq. (8)
 3: **for** $i \rightarrow \sigma$ **do**
 4: **fr** $i \rightarrow m$ **do**
 5: Generate random number γ
 6: Generate new sample y according to Eq.(9)
 8: **end for**
 9: **end for**
 10: Output new set of minority

IV. EXPERIMENTAL ANALYSIS

A. Collected Data

TABLE 1. Provide the characteristic of the data used in this work, which describe the name, number of features and the number of instances of the data. Its provides a different kind of the size and level of imbalance data. Also, these data are inspired from biomedical domains some of which are proprietary. Pima diabetes, Breast cancer and Thyroid disease (which contain a binary class) are all available through the UCI repository [1].

TABLE I. DATA CHARACTERISTICS

| no | Name | Instances | Features |
|----|-----------------|-----------|----------|
| 1. | Pima diabetes | 768 | 9 |
| 2. | Breast cancer | 699 | 11 |
| 3. | Thyroid disease | 3163 | 27 |

B. ACC Evaluation Measures

The confusion matrix is most powerful metrics that assess the performance of machine learning algorithm as shown in TABLE 2. The confusion matrix categorized into columns and rows that describe the prediction class and actual class respectively. The confusion matrix parameters are used to show the accuracy the classification algorithm. These four parameters are classified as follows TN (True Negatives), FP (False Positives), FN (False Negatives) and TP (True Positives). The positive instance most of them correctly classified, and the rest incorrectly classified. Furthermore, the negative instance most of them correctly classified, and the rest incorrectly classified. Generally, the equation of the classification accuracy or the prediction accuracy is calculated as illustrated in the following formula 6.

$$Acc = \frac{(TP + TN)}{(TP + FP + TN + FN)} \quad (10)$$

In term of the imbalanced data there two metrics are used as equal error costs and unequal error costs respectively. The error rate (Er) is calculated as most important tool that used to investigate the performance of these metrics, which calculated as illustrated in the formula 7.

$$E_r = 1 - accuracy \quad (11)$$

For the existence of the imbalanced data with unequal error cost, the area under the curve (ROC) is the most suitable metric used to tackle the imbalance data problem. There are similar techniques are presented by (Ling & Li, 1998; Drummond & Holte, 2000; Provost & Fawcett, 2001; Bradley, 1997; Turney, 1996). Finally, many works are presented with the term of ROC which supports the study of decision boundaries or relative costs of TP and FP. ROC metrics is coordinated on two axis as X-axis and Y-axis to calculate the %FP = FP/(TN+FP) of X-axis and %TP = TP/(TP+FN) of Y-axis respectively. The ROC provide a better performance on the point (0,100), which explain the correct instance and incorrect instance of the positive and negative class.

TABLE II. CONFUSION MATRIX

| | | Prediction | |
|--------|-----------------|--------------------|--------------------|
| | | Predicted Negative | Predicted Positive |
| Actual | Actual Negative | TN | TN |
| | Actual Positive | FN | TP |

C. AUC Evaluation Measures

The ROC curve can be easily shifted by manipulating the balance of training instance for each class in the training set. Area under the ROC Curve (AUC) is a helpful measure for classifier performance as it is independent of the decision criterion specified and previous probabilities. The AUC comparison can create a strong relationship between classifiers. If the ROC curves are overlapping, the total AUC is a mean comparison among the models (Lee, 2000). But, for certain cost and class distributions, the classifier have highest AUC may reality be sub-optimal. Thus, we also calculate the ROC convex hulls, since the points lying on the ROC convex hull are possibly ideal (Provost, Fawcett, & Kohavi, 1998; Provost & Fawcett, 2001).

The Classification Performance of FD_SMOTE technique with different percentages can be observed in the Tables 1, 2 and 3. Here it can observe from the all the tables the representation of the rows or classes in the dataset, the SMOTE technique analyze the percentage (%) of the majority and minority class for all three datasets. The majority represents the patients who are not affected by a disease and their features need to model. So to balance the minority class that requires increasing the minority sample by setting the percentage of SMOTE technique in multiples of 100 as follows:

TABLE III. SMOTE (%) OF PIMA DIABETIC

| SMOTE (%) | Majority Class | | Minority Class | | Total |
|---------------|----------------|-----|----------------|-----|-------|
| SMOTE % = 0 | 500 | 66% | 268 | 34% | 768 |
| SMOTE % = 100 | 500 | 48% | 536 | 52% | 1036 |
| SMOTE % = 200 | 500 | 38% | 723 | 62% | 1305 |

TABLE IV. SMOTE (%) OF BREAST CANCER

| SMOTE (%) | Majority Class | | Minority Class | | Total |
|---------------|----------------|-----|----------------|-----|-------|
| SMOTE % = 0 | 458 | 65% | 241 | 35% | 699 |
| SMOTE % = 100 | 458 | 49% | 482 | 51% | 940 |
| SMOTE % = 200 | 458 | 39% | 723 | 61% | 1181 |

TABLE V. SMOTE (%) OF THYROID DISEASE

| SMOTE (%) | Majority Class | | Minority Class | | Total |
|---------------|----------------|-----|----------------|-----|-------|
| SMOTE % = 0 | 2559 | 81% | 604 | 19% | 3163 |
| SMOTE % = 100 | 2559 | 68% | 1204 | 32% | 3767 |
| SMOTE % = 200 | 2559 | 58% | 1812 | 42% | 4371 |
| SMOTE % = 300 | 2559 | 58% | 2416 | 49% | 4975 |

The Performance evaluation of Pima diabetes data classification using FD_SMOTE technique can be observed in the tables 5 and 6. From the relationship of the accuracy (ACC), area under the curve (AUC), here the Table 5 and 6 shown that the ACC, AUC metrics generated with PCA and FD_SMOTE technique are better than the ACC metrics that

based feature (CFs) and information gain (InfoGs) technique in all classifiers methods. It reveals that the AUC metrics in all biomedical data is higher than other metrics.

TABLE VI. ACCURACY RESULT OF PIMA DIABETIC

| Classifiers | FD_SMOTE | CFs | InfoGs |
|-----------------|----------|---------|---------|
| MultiPerceptron | 88.1771 | 76.4323 | 76.7375 |
| SVM | 91.0156 | 71.0425 | 75.3906 |
| N Neighbor | 92.9863 | 76.0618 | 73.9583 |
| Bagging | 90.6094 | 74.0885 | 75.6510 |
| Random Forest | 91.8698 | 74.8698 | 72.7865 |
| Naïve Bayes | 89.6094 | 76.3672 | 74.8698 |

TABLE VII. AUC RESULT OF PIMA DIABETIC

| Classifiers | FD_SMOTE | CFs | InfoGs |
|-----------------|----------|-------|--------|
| MultiPerceptron | 0.998 | 0.723 | 0.815 |
| SVM | 0.971 | 0.719 | 0.827 |
| N Neighbor | 0.963 | 0.741 | 0.804 |
| Bagging | 0.989 | 0.805 | 0.820 |
| Random Forest | 0.997 | 0.812 | 0.800 |
| Naïve Bayes | 0.984 | 0.823 | 0.813 |

Figs. 3 and 4 illustrate the relationship of AUC and ACC of all classifiers algorithms for Pima diabetes classification. Here it can be observed that ACC and AUC metrics of PCA combined FD_SMOTE technique has better results compared with correlation based feature (CFs) and information gain (InfoGs) techniques.

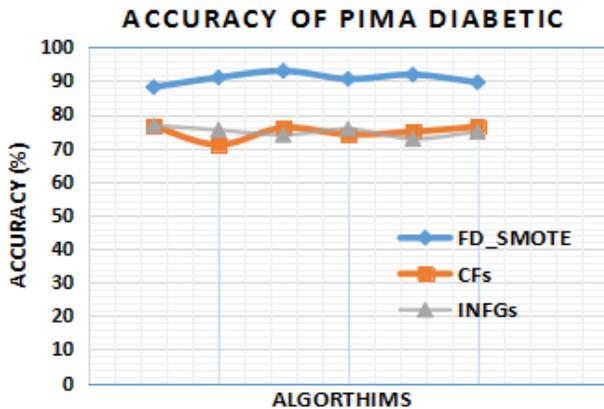


Fig. 2. ACC result of FD_SMOTE, CFs and InfoGs

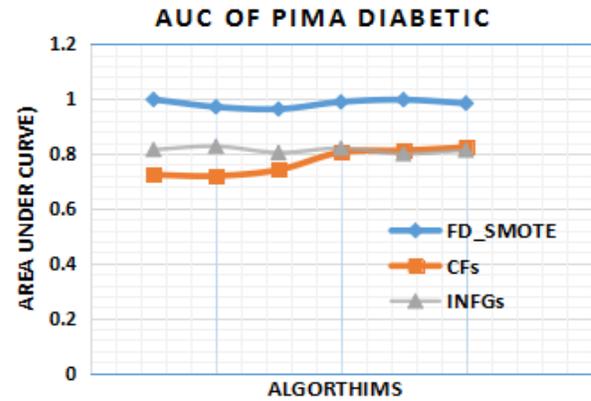


Fig. 3. AUC result of FD_SMOTE, CFs and InfoGs

The Performance evaluation of breast cancer data classification using FD_SMOTE technique can be observed in the tables 7 and 8. From the relationship of the accuracy (ACC), area under the curve (AUC), here the Table 7 and 8 shown that the ACC, AUC metrics generated with SMOTE technique are better than the ACC metrics that generated based feature (CFs) and information gain (InfoGs) techniques in all classifiers methods. It reveals that the AUC metrics in all biomedical data is higher than other metrics.

TABLE VIII. ACC RESULT OF BREAST CANCER

| Classifiers | FD_SMOTE | CFs | InfoGs |
|-----------------|----------|---------|---------|
| MultiPerceptron | 93.8072 | 81.4235 | 74.4206 |
| SVM | 96.6809 | 82.9957 | 86.4235 |
| N Neighbor | 95.6809 | 80.1373 | 85.9943 |
| Bagging | 94.7340 | 86.2804 | 75.9943 |
| Random Forest | 89.8404 | 79.7082 | 75.4220 |
| Naïve Bayes | 92.1184 | 82.1373 | 90.7082 |

TABLE IX. AUC RESULT OF BREAST CANCER

| Classifiers | FD_SMOTE | CFs | InfoGs |
|-----------------|----------|-------|--------|
| MultiPerceptron | 0.847 | 0.555 | 0.555 |
| SVM | 0.795 | 0.577 | 0.551 |
| N Neighbor | 0.759 | 0.581 | 0.535 |
| Bagging | 0.893 | 0.561 | 0.563 |
| Random Forest | 0.881 | 0.595 | 0.566 |
| Naïve Bayes | 0.894 | 0.586 | 0.571 |

Figs. 5 and 6 illustrate the relationship of AUC and ACC of all classifiers algorithms for breast cancer classification. Here it can be observed that ACC and AUC metrics of PCA combined FD_SMOTE technique has better results compared with correlation based feature (CFs) and information gain (InfoGs) techniques.

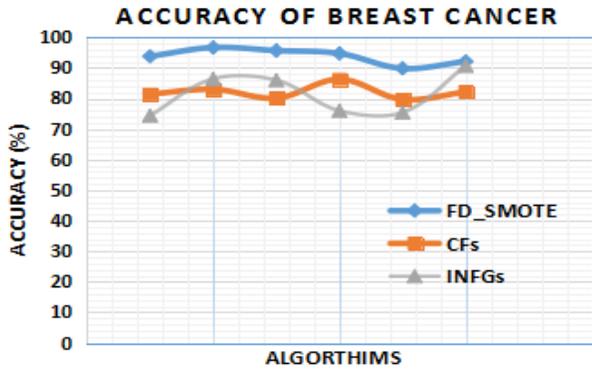


Fig. 4. AUC result of FD_SMOTE, CFs and InfoGs

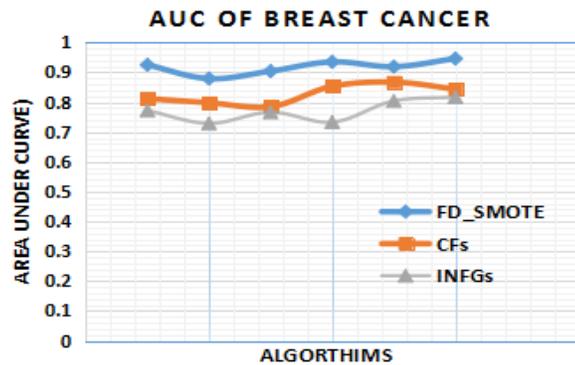


Fig. 5. AUC result of FD_SMOTE, CFs and InfoGs

The Performance evaluation of medical thyroid disease data classification using FD_SMOTE technique can be observed in the tables 9 and 10. From the relationship of the accuracy (ACC), area under the curve (AUC), here the Table 9 and 10 shown that the ACC, AUC metrics generated with SMOTE technique are better than the ACC metrics that based feature (CFs) and information gain (InfoGs) techniques in all classifiers methods. It reveals that the AUC metrics in all medical data is higher than other metrics.

TABLE X. ACC RESULT OF THYROID DISEASE

| Classifiers | FD_SMOTE | CFs | InfoGs |
|-----------------|----------|---------|---------|
| MultiPerceptron | 82.7228 | 56.2500 | 56.2500 |
| SVM | 84.1291 | 62.7315 | 65.2800 |
| N Neighbor | 77.1267 | 62.2685 | 58.7963 |
| Bagging | 84.1146 | 61.3426 | 64.3519 |
| Random Forest | 83.2176 | 66.2037 | 63.4259 |
| Naïve Bayes | 84.1291 | 59.9537 | 65.2778 |

TABLE XI. AUC RESULT OF THYROID DISEASE

| Classifiers | FD_SMOTE | CFs | InfoGs |
|-----------------|----------|-------|--------|
| MultiPerceptron | 0.925 | 0.812 | 0.772 |
| SVM | 0.879 | 0.798 | 0.729 |
| N Neighbor | 0.904 | 0.785 | 0.766 |
| Bagging | 0.935 | 0.853 | 0.733 |
| Random Forest | 0.919 | 0.867 | 0.804 |
| Naïve Bayes | 0.946 | 0.844 | 0.817 |

Figs. 7 and 8 illustrate the relationship of AUC and ACC of all classifiers algorithms for thyroid disease classification. Here it can be observed that ACC and AUC metrics of PCA combined FD_SMOTE technique has better results compared with correlation based feature (CFs) and information gain (InfoGs) techniques.

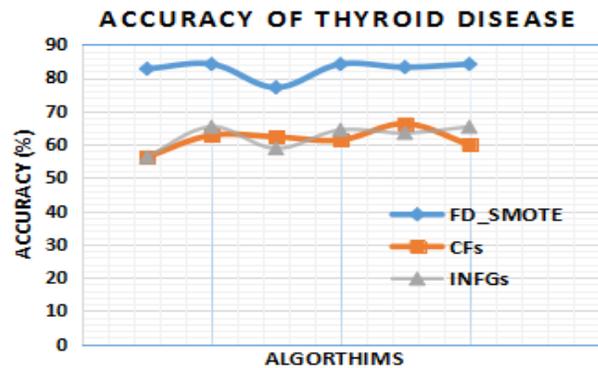


Fig. 6. AUC result of PCA and FD_SMOTE

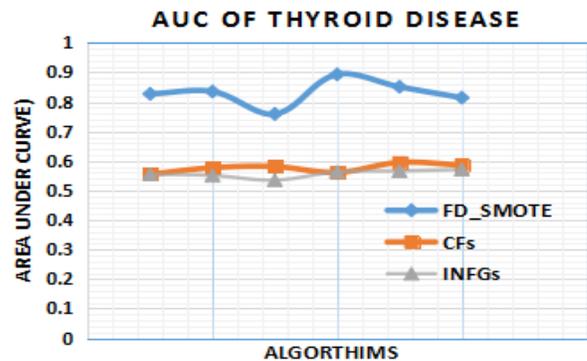


Fig. 7. AUC result of PCA and FD_SMOTE

V. CONCLUSIONS

In this paper a new algorithm has been proposed for generating an accurate classification of biomedical data. This aims to tackle the skewed data distribution and high dimensionality problem. The approach has been constructed by combing the PCA and FD_SMOTE based on farther sample. From the qualitative and quantitative analysis different classifiers based on PCA and FD_SMOTE has been used and it reveals that the new approach increases the performance of

(AUC) metrics and (ACC) metrics which used on a variety data of biomedical field. The present analysis shows that the combined technique is most effective than other existing approaches such as correlation based feature (CFs) and information gain (InfoGs). However the future plan is to investigate the present problem with rough set theory including the imbalanced data.

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